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The Crystal Structure **of** Ceric Ammonium Nitratel

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Received October 23, 1967

The crystal structure of ceric ammonium nitrate, $(NH_4)_2Ce(NO_3)_6$, has been determined from three-dimensional singlecrystal X-ray diffraction data collected by counter methods. The crystals are monoclinic, space group $P2_1/n$ with unit cell parameters $a = 13.061 \pm 0.007$, $b = 6.842 \pm 0.004$, $c = 8.183 \pm 0.004$ Å, $\beta = 91.34 \pm 0.02$ °, $\rho_0 = 2.49$, $\rho_0 = 2.490$ g/cm³ for $Z = 2$. Block-diagonal anisotropic least-squares refinement led to a conventional R of 0.036 for 625 observed reflections. The structure is composed of ammonium cations and hexanitratocerate anions. The hexanitratocerate anions result from the bidentate coordination of six nitrate groups about each cerium atom. The approximate symmetry is T_h . The average Ce-O distance is 2.508 \pm 0.007 Å, the average N-O distance involving a coordinated oxygen is 1.282 \pm 0.011 Å, and the average N-O distance involving a noncoordinated oxygen is 1.235 ± 0.011 Å.

Introduction

Ceric ammonium nitrate has been employed by analytical chemists for years as an oxidation standard. Moreover, it has recently been used as an oxidant in the conversion of various alcohols and toluenes to the corresponding aldehydes. 2^{-5} In some of these oxidations, nitratoaldehydes have been produced in high yields⁶ indicating participation of the nitrate groups of the oxidant in the oxidation mechanism. X-Ray diffraction studies of concentrated aqueous solutions of ceric ammonium nitrate indicate a coordination number of 12 for cerium' which could only be possible if the ligands are multidentate with a short bite. Since bidentate 12-fold coordination by nitrate groups has been found in the cerium(III) salt, $Ce₂Mg₃(NO₃)₁₂$. $24H₂O₁⁸$ it is not unreasonable to expect some kind of nitratocerate complex ions in aqueous solutions of ceric ammonium nitrate. It is, therefore, apparent that a complete understanding of the mechanisms of oxidation by ceric ammonium nitrate depends on knowledge of the structure of the reactant species. To obtain this structural information, a single-crystal X-ray diffraction investigation of ceric ammonium nitrate was undertaken.

Experimental Section

Crystals of ceric ammonium nitrate, $(NH_4)_2$ Ce(NO_3)₆, as obtained from the G. F. Smith Chemical Co. were small and badly twinned. Larger crystals were obtained by digesting the original material in concentrated nitric acid for several days. These larger crystals were also twinned, but a satisfactory single crystal was obtained by cleaving a twin with a razor blade. The visible satellite crystals were dissolved with a moist paper towel. The resultant single crystal was an almost perfect parallelepiped approximately 0.2 mm along each edge. The only visible forms were $\{101\}$ and $\{010\}$. Because of its deliquescence the crystal was mounted in a 0.2-mm soft-glass capillary with the *a** axis approximately collinear with the capillary axis.

Precession pictures made with Mo *Ka* radiation indicated monoclinic symmetry with systematic extinctions of $h0l$ reflections for $h + l$ odd and $0k0$ reflections for k odd. The space group is P2 $1/n$. The unit cell dimensions at 22° were obtained from a least-squares refinement by means of the program $LCR-2^{\circ}$ of the 20 settings of 18 reflections with $20 > 100^{\circ}$ which had been accurately centered on a General Electric diffractometer using Cr K_{α} radiation (λ 2.29092 Å for K_{α} and 2.28962 Å for K_{α_1}). The unit cell parameters are $a = 13.061 \pm 0.007$, $b = 6.842 \pm$ 0.004 , $c = 8.183 \pm 0.004$ Å, $\beta = 91.34 \pm 0.02^{\circ}$, $V = 731.1$ Å³. The estimated standard deviations include systematic errors in addition to random errors. The systematic errors were estimated by accounting for absorption and the residual error in the $2\theta = 0$ instrument setting, in the least-squares refinement. The density of the crystals as measured by flotation was 2.49 g/cm³; the density calculated with $Z = 2$ was 2.490 g/cm³. Space group $P2_1/n$ with $Z = 2$ requires $\overline{1}$ point symmetry for the cerium positions. The cerium atoms were, therefore, located at 0, 0, 0 and $\frac{1}{2}$, $\frac{1}{2}$, $\frac{1}{2}$, where they contribute only to the reflections for which $h + k + l = 2n$. These reflections were, indeed, significantly more intense than the $h + k + l = 2n + 1$ reflections on the precession and Weissenberg photographs.

A General Electric XRD-5 X-ray unit equipped with a singlecrystal orienter and scintillation counter was used with Mo K_{α} radiation $(\lambda 0.7107 \text{ Å})$ in the moving-crystal-moving-counter mode **(0, 20** coupling) to measure intensities. A 100-sec scan covering 3.33' was used for each reflection. Strong peaks were corrected for nonlinearity of the counting system by assuming a dead time of 10^{-5} sec. Individual backgrounds were measured by the same scanning procedure with ω offset by 1.8°. The takeoff angle was 3.0° and the diffracted beam aperture was 2.2° . Two standard reflections were monitored throughout the process of intensity measurement as a check for decomposition. Decomposition was negligible. Two crystallographically independent octants of data were measured out to $2\theta = 40^{\circ}$ ((sin θ)/ λ = 0.481) where the reflections for which $h + k + l = 2n + 1$ could not be distinguished above the background. Because these reflections result from the scattering of the light atoms only, it was assumed that the intensities of the reflections for which $h + k + l = 2n$ in this region of reciprocal space and beyond resulted only from cerium scattering. Since the positions of the ceriums had been determined by symmetry, data in the region 2θ > 40° were considered of little value and were not measured. Reflections were considered observed if, in addition to giving a definite peak on the recorder trace, $F_0 > 2\sigma(F_0)$ *(vide infra)*. **A** total of 690 reflections were recorded of which 625 were considered observed. An unobserved reflection having failed either of the above two tests was given a threshold value for F_0 equiva-

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⁽¹⁾ Work was performed in the Ames Laboratory *of* the U. S. Atomic Energy Commission.

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⁽⁵⁾ W. S. Trahanovsky, L. B. Young, and G. L. Brown, *ibid.,* **32,** 3865 (1967).

⁽⁶⁾ W. *S.* Trahanovsky, L. M. Smith, **and** P. J. Flash, 154th National Meeting of the American Chemical Society, Chicago, Ill., Sept 1967, Abstract S166.

⁽⁷⁾ R. D. Larsen and G. H. Brown, *J. Phys. Chem., 68,* 3060 (1964).

⁽⁸⁾ A. Zalkin, J. D. Forrester, and D. H. Templeton, *J. Chem. Phys.,* **39,** 2881 (1963).

lent to $2\sigma(F_o)$ or F_o , whichever was larger. Unobserved reflections were included in the least-squares refinement only if F_e was larger than the threshold F_o . Only three unobserved reflections had $F_{\rm e}$ > $F_{\rm o}$ and were included in the final cycle of refinement.

A streak correction10 mas applied to 38 reflections which occurred along densely packed radial reciprocal lattice rows. The approximate crystal dimensions and the linear absorption coefficient for Mo K_{α} radiation, $\mu = 33.4$ cm⁻¹, were used to compute absorption corrections." The transmission factors, *A* 's, which ranged from 0.446 to 0.620, mere applied along with the usual Lorentz-polarization corrections to reduce the intensities to structure factors. An attempt was made to account for systematic as well as random errors in the assignment of standard deviations to the intensity data. The formula used was

$$
\sigma(I) = \frac{1}{A} [C_{\rm T} + C_{\rm B} + C_{\rm S} + (K_{\rm T} C_{\rm T})^2 + (K_{\rm B} C_{\rm B})^2 + (K_{\rm S} C_{\rm S})^2 + (K_{\rm A} I)^2]^{1/2}
$$

where C_T , C_B , C_S , I , and A are, respectively, the total counts, background counts, streak counts, the intensity corrected for Lorentz-polarization and absorption effects, and the transmission factor. K_T , K_B , K_S , and K_A are, respectively, the estimated errors in the total counts, background counts, streak counts, and the transmission factor. Based on experience in this laboratory, K_T and K_B were assigned values of 0.02; K_S , 0.10; and K_A , 0.03. $\sigma(F)$ was computed from $\sigma(I)$ for each reflection by the method of finite differences¹⁰

$$
σ(F) = (Lp)^{-1/2}([I + σ(I)]1/2 - I1/2)
$$

Structure Determination

If the cerium atoms are considered alone, the structure is body centered. A straightforward application of the heavy-atom method would, therefore, lead to a body-centered structure which would obviously be the superposition of the true structure and its image after rotation by 180" about the *b* axis. Chemical intuition mould probably permit one to extract the true structure from the result; however, the direct method¹²⁻¹⁶ appeared to offer an easier solution in this case.

The scattering factors used in this investigation were those of Hanson, *et al.*,¹⁷ for neutral N and also O. The Ce^{4+} scattering factor of Thomas and Umeda¹⁸ was used for cerium. The effects of anomalous dispersion are reasonably expected to be minimal in this structure. The only anomalous scatterer is the cerium atom which, because of its location at a center of symmetry, contributes an approximately constant imaginary component of 3.0 electrons to only half of the structure factors. In view of these considerations, as well as the uncertainty in values for f' and f'' , anomalous dispersion was neglected. The only structural parameters which could be affected are the temperature factors for the Ce atom. Ceric ammonium nitrate is obviously not a structure of equal scatterers as is presumed

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by Sayer's equation,¹² but this difficulty is easily avoided by subtracting the contribution due to the cerium atoms from each reflection for which $h + k + l = 2n$ under the assumption that the signs of these reflections are all plus. In order to subtract the cerium contribution, however, the scale factor, which can be determined by Wilson's method, **l9** must be accurately known. Wilson's method also depends on the assumption of a random structure of equal scatterers, but this is altogether reasonable for the $h + k + l = 2n + 1$ reflections to which the cerium atoms do not contribute. The data were, therefore, divided into two sets according to the parity of $h + k + l$. The light-atom reflections $(h + k + l = 2n + 1)$ were scaled in the usual way and yielded a scale factor of 0.2904 and an isotropic temperature factor of 3.44. For the cerium reflections $(h + k + l = 2n)$, the contribution of the cerium to each reflection is $2f_{\text{Ce}}$. Consequently, $4f_{Ce}^2$ was added to $\Sigma_i f_i^2$ for the light atoms in the scaling of the cerium reflections. The scale factor for these reflections was 0.3553; the isotropic temperature factor, 1.37. The scale factors agree rather well, and the geometric mean, 0.321, was used along with the isotropic temperature factor, 1.37, due mainly to the cerium, to subtract the scattering power of the ceriums from all of the cerium reflections. The scale factor as determined in the final least-squares cycle was 0.3292 ; the final isotropic temperature factor for cerium was 1.82.

The data were then recombined, rescaled, and reduced to a set of normalized unitary structure factors, *E's.20* The distribution of the *E's* is given in Table I.

The 78 *E's* which were greater than 1.5 were arranged in the usual Sayer relationships. Thirty-five of these *E*'s (those for which $h + k + l = 2n$) had signs determined in the subtraction of the cerium scattering. Ordinarily in monoclinic crystals three signs can be assigned arbitrarily to reflections of three independent parity groups to determine the origin of the unit cell.¹⁶ Two of these degrees of freedom, however, were used in the selection of 0, 0, 0 and $\frac{1}{2}$, $\frac{1}{2}$, $\frac{1}{2}$ as cerium positions from among the four equivalent sets of special positions in space group $P2_1/n$. The one remaining degree of freedom represents the selection of either $0, 0, 0$ degree of Heedom represents the selection of either σ , σ , σ or $\frac{1}{2}$, $\frac{1}{2}$, $\frac{1}{2}$, $\frac{1}{2}$ as the origin. Thus, one of the reflections, for which $h + k + l = 2n + 1$, 450, was given a plus sign. The signs of 20 light-atom reflections were obtained by checking for consistency in the Sayer rela-

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⁽¹¹⁾ W. R. Busing and H. A. Levy, *Acta fiyst.,* 10, 180 (1957).

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⁽²⁰⁾ This and subsequent calculations, unless otherwise noted, were performed on an IBM 360 Model 50 computer with the crystallographic programs written by F. R. Ahmed, S. R. Hall, M. E. Pippy, and C. P. Saunderson of the National Research Council, Ottawa, Ontario, Canada.

TABLE 11

 ϵ shave the form: $\exp[-(b_{11}h^2 + b_{22}k^2 + b_{32}l^2)]$ $b_{23}kl$).

tionships. The sign of one cerium reflection appeared inconsistent and was removed from the data set. There remained *55 E's* for which signs had been determined. These reflections were used to compute an *E* map in which 12 of the 13 light atoms were visible. The coordinates of these 12 light atoms (all but $O(12)$) were used as starting parameters along with the ceriums for two isotropic block-diagonal least-squares cycles, one utilizing only low-angle data; the second, all data. An electron density map was then computed which clearly showed the remaining oxygen.

The structure was refined by block-diagonal leastsquares techniques with the NRC least-squares program which minimized the function $\sum w(|F_o| - |F_o|)^2$. For each isotropic atom one 4×4 block containing positional parameters and the isotropic temperature factor was used. Two blocks were used for each anisotropic atom. The first was a 3×3 block of positional parameters; the second, a 6×6 block of anisotropic temperature factors. The weighting scheme was $\sqrt{w} = \sigma(F)^{-1}$. Unobserved reflections were weighted exactly the same as observed reflections if $F_e \geq F_o$. They were, however, given weights of zero if $F_{\rm e} < F_{\rm e}$. With all atoms given isotropic temperature factors the refinement led to a conventional *R* factor, factors the refinement led to a conventional *R* factor,
 $R_1 = \Sigma(|F_o| - |F_e|)/\Sigma|F_o|$, of 0.049 and a weighted *R* $R_1 = \Sigma(|F_o| - |F_o|)/\Sigma|F_o|$, of 0.049 and a weighted R
factor, $R_2 = (\Sigma w(|F_o| - |F_o|)^2/\Sigma wF_o^2)^{1/2}$, of 0.064. When the ceriums were given anisotropic temperature factors and all other atoms remained isotropic, R_1 was reduced to 0.044 ; R_2 , to 0.061 . With all atoms anisotropic, $R_1 = 0.036$ and $R_2 = 0.050$. The average shift was 0.07σ ; the maximum shift was 0.3σ in the final cycle. The average standard deviation of an observation of unit weight was 2.68 which indicates a slight underestimation of errors. Using Hamilton's²¹ significance test, both the hypothesis that all atoms are isotropic as well as the hypothesis that all but the ceriums are isotropic can be rejected at the 0.005 level. The final positional and thermal parameters along with their estimated standard deviations are listed in Table 11. Experience in this laboratory indicates

that the block-diagonal approximation leads to standard deviations which are consistently underestimated by a factor of 0.8. Consequently the standard deviations listed in Table I1 as well as all estimated errors derived from them should be multiplied by 1.2 to correspond with values derived from the more conventional full-matrix least-squares techniques. The structure factors computed from these parameters are compared with the observed values in Table 111. **A** comparison of the observed and calculated *F's* for the more intense reflections indicated the absence of extinction effects. Consequently, no extinction correction was made. Two reflections, 202 and -426 , showed large discrepancies between calculated and observed *F's.* These reflections were remeasured and yielded the same results. Reflection 202 was obviously absent on the precession photographs. It was therefore concluded that the peak recorded on the diffractometer resulted from a multiple reflection, and it was given a weight of zero in the least-squares refinement. Reflection -426 was listed as unobserved because $F_{\rm o}$ < 2 $\sigma(F)$, whereas a well-defined peak appeared on the recorder trace. This error presumably resulted from an anomalously high background measurement possibly including the white streak from another reflection. This reflection was also given a weight of zero.

A difference Fourier map was computed at the conclusion of the refinement in an attempt to locate the hydrogens. The largest peaks, both positive and negative, occurred in the vicinity of the cerium position and ranged from -0.4 to 1.1 e/Å³. Elsewhere, the noise level was about $0.2 e/\text{\AA}^3$. There was an area of positive density 0.2 e/Å³ around N(14), but chemically reasonable hydrogen positions could not be assigned.

Results

Ceric ammonium nitrate is composed of ammonium cations and hexanitratocerate anions in which the nitrate groups are apparently tightly held by the cerium atoms. The symmetry of the hexanitratocerate ion closely approximates T_h with a $\overline{3}$ axis parallel to the TABLE **¹¹¹**

OBSERVED AND CALCULATED STRUCTURE FACTORS[®]

Each group of data is headed with values for *h* and *l*. Within each group are listed k , $10F_0$, and $10F_0$, respectively. The signs of the F_6 's are the calculated signs. A negative F_0 indicates a threshold value for an unobserved reflection. Those reflections which have an asterisk after *F,* were omitted from the least-squares refinement,

Figure 1.—Hexanitratocerate anion. The numbering scheme is indicated by numbering the atoms closest to the viewer. These positions differ from those in the coordinate list in that these are the atoms which result by inverting the original positions through the center of symmetry at the cerium position. The b axis points out of the plane of the paper, the a axis points upward, and the c axis points from left to right.

crystallographic *b* axis. The structure of this ion is indicated in Figure 1, which was prepared by the computer utilizing Johnson's ORTEP program.22 The bond distances and angles are listed in Tables IV and V. The standard deviations as computed from the block-diagonal least-squares matrix are 0.007 A for Ce-O distances, 0.011 Å for N-O distances, 0.2° for 0-Ce-0 angles, and 0.6" for 0-K-0 angles. The bond distance from the nitrogen to the noncoordinating

oxygen is significantly shorter than the other N-0 distances in each nitrate group. Since these oxygens apparently have the largest rms amplitudes of thermal vibration, the bond distances were corrected for thermal motion by means of the ORFFE²³ program under the assumption that 0 rides on N for the N-0 bonds and that O rides on Ce for the Ce-O bonds.²⁴ The direction cosines for the principal axes of thermal

⁽²²⁾ C. K. Johnson, "ORTEP, a Fortran Thermal-Ellipsoid Plot Program for Crystal Structure Illustrations," Oak Ridge National Laboratory, **Oak** Ridge, Tenn., Report *So.* OKNL *37'3* 1.

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⁽²⁴⁾ W. R. Busing and H. A. Levy, *Acta Cryst.*, **17**, **1**42 (1964).

TABLE IV BOND DISTANCES (Å) IN CERIC AMMONIUM NITRATE^a

Bond	Uncor for therm vib therm vib	Cor^b for	Bond	Uncor for therm vib therm vib	Cor^b for
$Ce(1)-O(3)$	2.490	2.497	$N(2)$ –O(3)	1.271	1.280
$Ce(1)-O(4)$	2.524	2.530	$N(2)$ –O(4)	1.284	1.287
$Ce(1)-O(7)$	2.506	2.510	$N(2)-O(5)$	1.218	1.243
$Ce(1)-O(8)$	2.482	2.488	$N(6)-O(7)$	1.266	1.272
$Ce(1)-O(11)$	2.509	2.514	$N(6)-O(8)$	1.283	1.289
$Ce(1)-O(12)$	2.504	2.512	$N(6)-O(9)$	1.210	1.235
			$N(10)-O(11)$	1.272	1.280
			$N(10)-O(12)$	1,286	1.286
			$N(10)-O(13)$	1.199	1.225
Av		$2.503 \pm 2.508 \pm$			

 0.015^o 0.014

a Standard deviations are ± 0.007 Å for Ce-O bonds and ± 0.011 Å for N-O bonds. ^b Ce-O distances, correction made on basis that oxygen atoms ride on cerium; N-0 distances, oxygens assumed to ride on nitrogens. *0* Error is the root-mean-square deviation for equivalent distances, *i.e.*, $\sqrt{2(x - \bar{x})^2/(n - 1)}$.

TABLE V

BOSD ANGLES (DEG) IN CERIC AMMONIUM NITRATE"

$O(3)$ -Ce (1) -O (4)	50.9	$O(4)45504 - N(14) - O(5)65602c$	65.4
$O(7)-Ce(1)-O(8)$	50.9	$O(4)45504 - N(14) - O(8)55501$	124.2
$O(11) - Ce(1) - O(12)$	50.6	$O(4)45504 - N(14) - O(9)55503$	149.0
$O(3) - Ce(1) - O(7)$	66.5	$O(4)45504 - N(14) - O(12)45404$	115.9
$O(3) - Ce(1) - O(8')^b$	69.9	$O(4)45504 - N(14) - O(13)55603$	96.4
$O(3) - Ce(1) - O(11)$	66.6	$O(5)65602 - N(14) - O(8)55501$	86.7
$O(3)$ -Ce (1) -O (12)	65.4	$O(5)65602 - N(14) - O(9)55503$	140.3
$O(4)-Ce(1)-O(7)$	65.1	$O(5)65602 - N(14) - O(12)45404$	89.6
$O(4) - Ce(1) - O(8')$	67.5	$O(5)65602 - N(14) - O(13)55603$	161.8
$O(4) - Ce(1) - O(11')$	67.5	$O(8)$ 55501-N (14) -O (9) 55503	58.5
$O(4)$ –Ce (1) – $O(12')$	69.0	$O(8)$ 55501-N(14)-O(12)45404	110.9
$O(7)-Ce(1)-O(11)$	69.2	$O(8)$ 55501-N(14)-O(13)55603	103.9
$O(7)-Ce(1)-O(12')$	66.8	$O(9)$ 55503-N (14) -O (12) 45404	86.1
$O(8)-Ce(1)-O(11)$	65.0	$O(9)55503 - N(14) - O(13)55603$	56.6
$O(8)-Ce(1)-O(12')$	68.3	$O(12)45404 - N(14) - O(13)55603$	100.0
$O(3)-N(2)-O(4)$	115.2		
$O(3)-N(2)-O(5)$	124.1		
$O(4)-N(2)-O(5)$	120.7		
$O(7)-N(6)-O(8)$	114.6		
$O(7)-N(6)-O(9)$	124.5		
$O(8)-N(6)-O(9)$	120.9		
$O(11) - N(10) - O(12)$	113.9		
$O(11) - N(10) - O(13)$	125.6		
$O(12) - N(10) - O(13)$	120.5		

^a The standard deviations are 0.2° ror O-Ce-O angles and 0.6° for $O-N-O$ angles. $\frac{b}{b}$ The primes indicate atoms inverted through the center of symmetry at the cerium position. *0* These are the angles about the ammonium ion which represent possible hydrogen bonds. Each atom number except the vertex atom is followed by the atom designator code which defines the symmetry operation which relates the atom to the original coordinates. See text for description of atom designator code.

vibration along with the root-mean-square displacements are tabulated in Table VI.

If the symmetry of the anion were exactly T_h , the nitrate groups would define three mutually perpendicular planes. The least-squares planes for the nitrate groups are given in Table VII. These planes were calculated with each atom given unit weight. Since the distances of the atoms from these planes are all about an order of magnitude smaller than their standard deviations, the nitrate groups are definitely planar. As can be seen from the equations, the sense of the normals to these planes is such that each normal has a positive component along the crystallographic *b* axis. The angles between these planes are: plane 1 plane *2,* 94.75'; plane 1-plane 3, 96.39'; plane *2-*

^{*a*} The direction cosines *l*, *m*, and *n* are referred to an orthonormal coordinate system the axes of which are parallel to the crystallographic *a, b,* and c* axes, respectively.

plane 3, 96.19'. The central cerium atom deviates by -0.3259 , -0.1301 , and -0.3679 Å from planes 1, 2, and **3,** respectively.

Discussion

The averages of chemically equivalent bond distances, corrected for thermal vibration. are compared in Table VI11 with the distances found in the solution study of ceric ammonium nitrate' and the single-crystal investigations of $Ce₂Mg₈(NO₃)₁₂·24H₂O⁸$ and cerium(IV) acetylacetonate.²⁵ It is immediately apparent that the Ce-O distances are 0.13 Å shorter in ceric ammonium nitrate than in Ce₂Mg₃(NO₃)₁₂ 24H₂O but 0.11 Å longer than in the eight-coordinated cerium (IV) acetylacetonate. That the Ce-0 distances are shorter

(26) B. **Matkovic and** D **Grdenic** *Ac'n Cvyst.,* **16, 456** (1962).

TABLE VI1 LEAST-SOULDES PLANES FOR NITRATE GROUPS

^aThe standard deviations of distances from the plane are *0.008* Å for nitrogens and 0.007 Å for oxygens. \bar{b} These equations refer to an orthonormal coordinate system defined by vectors parallel to the crystallographic axes a, b , and c^* . The parameters X, Y , and *2* are in Angstrom units.

Figure 2.—Locations of possible hydrogen bonds about $N(14)$. The atom designator codes have been left out of this drawing since the atom numbers uniquely define the atoms. The corresponding atom designator codes are listed in Table IX.

number *SN*. For the identity operation, $SN = 1$; for inversion through the center *o€* symmetry at 0, 0, 0, $SN = 2$; for rotation and translation by the $2₁$ screw at $x = \frac{1}{4}$, $z = \frac{1}{4}$, $SN = 3$; and for reflection and translation by the *n*-glide plane at $y = \frac{1}{4}$, $SN =$ 4. Atoms in neighboring unit cells are designated by crystal lattice translation digits, *T24, TB,* and *TC.* The origin is designated by zeros for all three digits.

TABLE VIII

			AVERAGE BOND DISTANCES (A)		
Soln Cerium(IV)					Sum of Slater
Bond	This work	$study^a$	$Ce2Mg3(NO3)12 \cdot 24H2Ob$	acetylacetonate ^c	radii ^d
$Ce-O$	2.508 ± 0.007	2.85	2.642 ± 0.005	2.40 ± 0.03	2.45
All $N-O's$	1.267 ± 0.011	1.35	1.263 ± 0.008		125
$N-O$ (coordinated) ^e	1.282 ± 0.011		1.271 ± 0.008		
$N-O(\text{lone})^f$	1.235 ± 0.011		1.246 ± 0.008		

a R. D. Larsen and G. H. Brown, *J. Phys. Chem.*, 68, 3060 (1964). *b* A. Zalkin, J. D. Forrester, and D. H. Templeton, *J. Chem. Phys.*, 39, 2881 (1963). *e B. Matkovic and D. Grdenic, Acta Cryst.*, 16, 456 (1962). *d* J. C. Slater, *J. Chem. Phys.*, 41, 3199 (1964). *e* Coordinated O refers to those oxygens which are bonded to the cerium atom. *I* Lone O is the remaining uncoordinated oxygen.

in the cerium(1V) compounds with respect to the cerium(II1) compounds is expected since the electronic configuration of cerium (IV) is that of the noble gas xenon while cerium(II1) has one additional electron. The difference between the two cerium (IV) compounds probably results from increased steric interactions in the 12-coordinated compound when compared with the 8-coordinated compound. The larger Ce-0 distances found in the solution study are impossible to assess since very few details and no standard deviations were given in that report.'

Even with correction for thermal vibration, the *S-0* distances to the noncoordinated oxygen atoms are significantly shorter than to the coordinated oxygens as shown in Table VIII. Since the inequality of $N-O$ distances has been observed in $Ce₂Mg₃(NO₃)₁₂·24H₂O⁸$ and in several other structures^{26,27} as well, there is little doubt that it is a real effect. This is probably a lengthening of the N-0 bonds to the coordinating oxygens due to the reduction of bond order which accompanies donation of electron density from these bonds to the Ce-0 bonds.

In discussing hydrogen bonding and interionic nonbonded distances the convention of Johnson²² is used. Each symmetry operation is assigned a symmetry

⁽²⁶⁾ T. Ueki, **A.** Zalkin, and U. H. Templeton, *Acta C~yst.,* **20,** *836* (1966). **(27)** J. *C.* Taylor, M. **13.** Muellcr, and 11. L. Hitterman, *ibid.,* **20,** ⁸⁴² **(1966).**

		HYDROGEN-BOND DISTANCES AND ALL		
		NONBONDED INTERIONIC DISTANCES LESS THAN 3.5 \AA		
Possible hydrogen-bond distances about $N(14)^a$		Nonbonded interionic distances less than 3.500 A^a		
N(14)–O(5)65602	2.933	$N(2)-O(9)55504$	3.005	
$N(14)-O(8)55501$	2.953	$N(2)$ -O(11)65602	3.465	
$N(14)-O(13)55603$	2.965	$O(3)-O(9)65602$	2.985	
$N(14)-O(4)45504$	3.004	$O(3)-O(9)55504$	3.256	
$N(14)-O(9)55503$	3.040	$O(3)-N(6)65602$	3.285	
$N(14)-O(12)45404$	3.062	$O(3)-O(7)65602$	3.372	
		$O(4)-O(5)65503$	3.209	
		$O(4)-N(14)66602$	3.354	
		$O(4)-O(9)55504$	3,479	
		$O(5)-O(13)55404$	2.984	
		$O(5)-O(9)55504$	3.054	
		$O(5) - N(10)55404$	3.061	
		$O(5)-O(11)65602$	3.168	
		$O(5)-O(11)55404$	3.439	
		$N(6)-O(13)55401$	3.307	
		$O(7)-O(13)65602$	3.152	
		$O(7)-O(11)65602$	3.309	
		$O(7)-N(14)55404$	3.330	
		$O(7)-N(10)65602$	3.381	
		$O(7)-O(13)55401$	3.497	
		$O(8)-O(9)55503$	2.931	
		$O(9)-O(13)55401$	2.846	
		$N(10)-N(14)55504$	3.428	
		$O(11) - N(14)55501$	3.348	
		$O(13)-O(13)65702$	3.072	

TABLE IX

^{*a*} The first atom listed for each distance has $ADC = 55501$. See text for description of ADC .

 $O(13) - N(14)55504$

3,178

Figure 3. Packing diagram of ceric ammonium nitrate. The b axis points out of the plane of the paper.

Translation in the positive direction one unit cell along the *a* axis makes $TA = 1$ and similarly for the other two axes. The atom designator code, *ADC,* is

 $ADC = (TA + 5) \times 10^4 + (TB + 5) \times 10^3 +$ $(TC + 5) \times 10^2 + SN$

Hence, the original parameters operated on only by the identity operator have $ADC = 55501$.

Six NH₄-O distances range from 2.933 to 3.062 Å; the next closest oxygen is 3.178 Å from N(14). The first six distances indicate the locations where hydrogen bonds are possible, but the seventh results from the fact that the oxygen is on the same nitrate group as the oxygen involved in the 3.062 Å distance. These distances along with the important nonbonded distances are listed in Table IX. Either the hydrogens are disordered or two of them must be involved in bifurcated hydrogen bonds. Since the hydrogens could not be located in the difference map, possibly the result of the first alternative, it is not possible to distinguish between these two possibilities. The arrangement of the six oxygens about $N(14)$ is shown in Figure 2.

If $O(13)55603$ and $O(9)55503$ shared one hydrogen and $O(8)55501$ and $O(5)65602$, another, the hydrogens could approach a tetrahedral arrangement about N(14). Each hexanitratocerate ion is involved in 12 hydrogen bonds as indicated in Figure 3. The coordinating oxygens can be divided into two groups. The first group includes 0(4), *0(8),* 0(12), and the corresponding atoms related to these by the center of symmetry at the cerium position. These atoms are close to the equator of the hexanitratocerate ion when the *5* axis parallel to the crystallographic *h* axis is chosen as the polar axis. Oxygens of the first group are referred to as equatorial oxygens. The second group includes $O(3)$, $O(7)$, $O(11)$, and the centrosymmetrically related atoms. These atoms are closest to the polar axis and are called polar oxygens. Every equatorial oxygen is involved in a hydrogen bond, whereas no polar oxygen is hydrogen bonded. Each noncoordinating oxygen is also hydrogen bonded primarily in the direction of the *b* axis. In this way the structure is held together by a three-dimensional network of hydrogen bonds.